

# Optimization of the ROCA (CVE-2017-15361) Attack

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- 2017 Czech researchers find flaw in Infineon's key generation algorithm<sup>1</sup>
- 750 000 Estonian ID-cards affected
- 140.8 CPU-years to factor an Estonian ID card (worst case)
- New result: 70.4 CPU-years to factor an Estonian ID card (worst case)
- New result: For 90 % of keys, average case is 4x better than ROCA paper

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<sup>1</sup>[https://crocs.fi.muni.cz/public/papers/rsa\\_ccs17](https://crocs.fi.muni.cz/public/papers/rsa_ccs17)

# Facts about the ROCA attack

- Factorization of RSA keys
- Takes advantage of the polynomial form of primes
- Prime number construction:  $p = k * M + (65537^a \bmod M)$
- Vulnerable variant of Joye and Paillier's secure prime generation algorithm<sup>2</sup>
- Key format:

$$N = \overbrace{(k * M + (65537^a \bmod M))}^p * \overbrace{(l * M + (65537^b \bmod M))}^q$$

- Fingerprintable:  $N \equiv 65537^{a+b} \bmod M \equiv 65537^c \bmod M$

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<sup>2</sup><http://joye.site88.net/papers/JPV00gen.pdf>

# Transfer entropy from $a$ to $k$

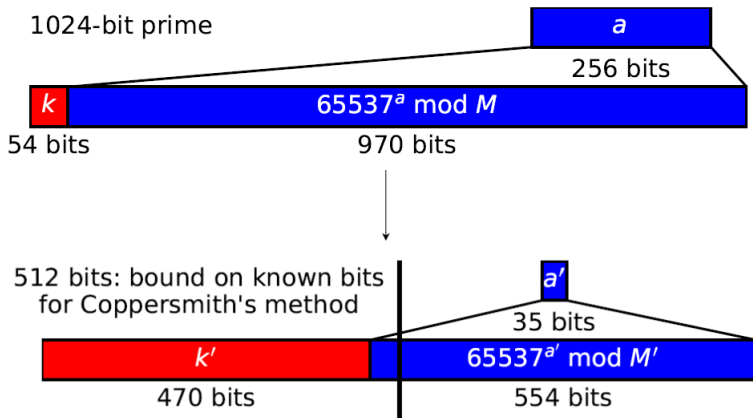


Figure: Prime form transformation<sup>3</sup>

<sup>3</sup>[https://crocs.fi.muni.cz/\\_media/public/papers/nemec\\_roca\\_csaw\\_poster.pdf](https://crocs.fi.muni.cz/_media/public/papers/nemec_roca_csaw_poster.pdf)

# Overview of the ROCA attack

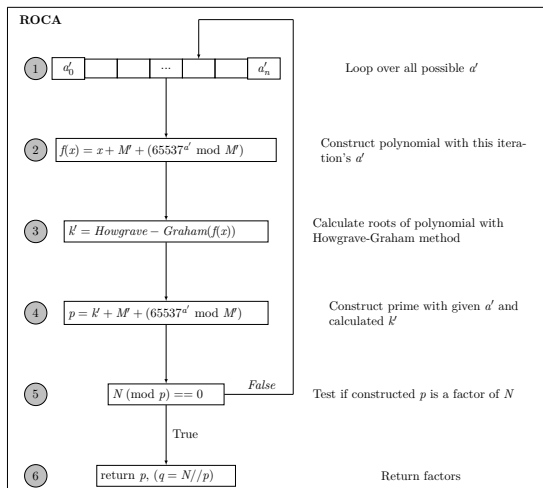


Figure: Overview of the ROCA attack

# Entropy of $a$ and $k$

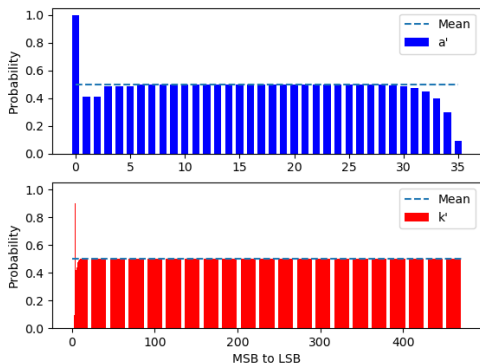


Figure: Entropy of each bit in  $a'$  and  $k'$ , MSB to LSB (2048-bit keys)

# Impact of the Optimizations

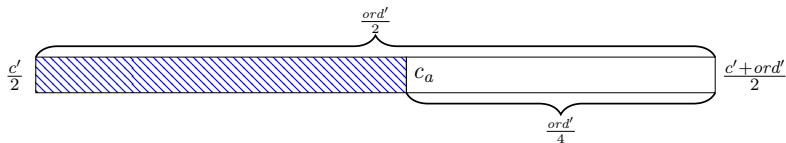


Figure: Comparison of the original and the new bruteforce range

$$p = \overbrace{(c_k + r)}^{k'} * M' + (65537^{a'} \bmod M') \quad (1)$$



<b>Key size</b>	<i>Non-optimized</i>	<i>Optimized</i>	<i>Optimized Random key</i>	<i>Optimized Cherry-picked</i>
<b>512-bit</b>	2.0333 CPU-hours*	2.2 CPU-hours	0.73 CPU-hours*	0.51 CPU-hours*
<b>1024-bit</b>	102.4 CPU-days	51.2 CPU-days	36.5 CPU-days	25.6 CPU-days
<b>2048-bit</b>	161.2 CPU-years	80.6 CPU-years	57.5 CPU-years	40.3 CPU-years (336\$)

Table: Efficiency of the ROCA attack using HPC

- <https://blog.cr.yo.to/20171105-infineon3.txt>
  - Attack with known  $a$
  - Not using  $M'$  transformation (not needed when known  $a$ )
- <https://github.com/brunoproduit/roca>
  - First publicly available full attack
  - Based on SageMath

```
$ python2 roca.py data/512.pem
[+] Importing key
[+] Key is vulnerable!
[+] RSA-512 key
[+] N = 80474497870208039394761476993787283293147334261
64267535316072793294233587337682475529099270039635820
022607073710171609979448215488148758894001678423611389
[+] c' = 588970
[+] Time for 1 coppersmith iteration: 0.04 seconds
[+] Estimated (worst case) time needed for the attack:
4 hours, 30 minutes and 3.46 seconds
[+] Found factors of N:
[+] p = 893165853412392001031647986291682301859833465485
58222489515734210664382833579
[+] q = 901002849165701396384390284897352814133860742044
03670730318637933879173958391
[+] Took 7742.3 s
[+] Exporting key to priv.pem
```

Listing 1: Execution of the attack against vulnerable key

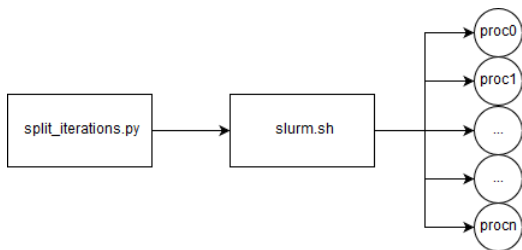


Figure: Splitting range for process allocation with given CPU cores available